

Projekt badawczy Narodowego Centrum Nauki pt.:

*Optymalizacja topologiczna konstrukcji inżynierskich. Ujęcie syntetyzujące metody: projektowania anizotropii z wolnego wyboru, projektowania materiałów niejednorodnych oraz metodę siatek typu Michella,*

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Politechnika Warszawska; Wydział Inżynierii Lądowej,

środki przyznane: 772 040 zł,

zajął 5. miejsce spośród 188 projektów złożonych w ramach konkursu: OPUS, Panel ST 8 (data ogłoszenia: 16 IX 2013 r.). Do drugiego etapu zakwalifikowano 47 wniosków; do finansowania skierowano 32 wnioski.

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NCN a Politechniką Warszawską.

Nr projektu: 2013/11/B/ST8/04436

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### **Publikacje (2014-2017)**

#### **1 Książka w opracowaniu**

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#### **2 Publikacje w periodykach**

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